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Abstract

Long-term gridded precipitation products are crucial for several applications in hydrology, agriculture and climate sciences. Currently available precipitation products suffer from space and time inconsistency due to non-uniform density of ground networks and the difficulties in merging multiple satellite sensors. The recent “bottom up” approach that exploits satellite soil moisture observations for estimating rainfall through the SM2RAIN algorithm is suited to build consistent rainfall data record as a single polar orbiting satellite sensor is used.

We exploit here the Advanced SCATterometer (ASCAT) on board three Metop satellites, launched in 2006, 2012 and 2018, as part of the EUMETSAT Polar System programme. The continuity of the scatterometer sensor is ensured until mid-2040s through the Metop Second Generation Programme. Therefore, by applying SM2RAIN algorithm to ASCAT soil moisture observations, a long-term rainfall data record will be obtained, starting in 2007 until mid-2040s. The paper describes the recent improvements in data pre-processing, SM2RAIN algorithm formulation, and data post-processing for obtaining the SM2RAIN-ASCAT quasi-global (only over land) daily rainfall data record at 12.5 km sampling from 2007 to 2018. The quality of SM2RAIN-ASCAT data record is assessed on a regional scale through the comparison with high-quality ground networks in Europe, United States, India and Australia. Moreover, an assessment on a global scale is provided by using the Triple Collocation technique allowing us also the comparison with the latest ECMWF reanalysis (ERA5), the Early Run version of the Integrated Multi-Satellite Retrievals for Global Precipitation Measurement (IMERG), and the gauge-based Global Precipitation Climatology Centre (GPCC) products.

Results show that the SM2RAIN-ASCAT rainfall data record performs relatively well both at regional and global scale, mainly in terms of root mean square error when compared to other products. Specifically, SM2RAIN-ASCAT data record provides performance better than IMERG and GPCC in the data scarce regions of the world, such as Africa and South America. In these areas, we expect the larger benefits in using SM2RAIN-ASCAT for hydrological and agricultural applications. Limitations of SM2RAIN-ASCAT data record consist in the underestimation of peak rainfall events and in the presence of spurious rainfall events due to high frequency soil moisture fluctuations that might be corrected in the future with more advanced bias correction techniques.

The SM2RAIN-ASCAT data record is freely available at https://doi.org/10.5281/zenodo.2591215.
Introduction

Rainfall is ranked the first among the Essential Climate Variable by the Global Climate Observing System (GCOS) as it represents the most important variable in many applications in geosciences (Maggioni and Massari, 2018). Long-term rainfall records are essential for drought monitoring (e.g., Forootan et al., 2019), water resources management (e.g., Ahera et al., 2017) and climate studies (e.g., Herold et al., 2016; Pendergrass and Knutti, 2018) while near real-time rainfall data are needed for the mitigation of the impacts of natural disasters such as floods and landslides (e.g., Wang et al., 2017; Camici et al., 2018; Brunetti et al., 2018; Kirschbaum and Stanley, 2018). Additional applications in which near real-time rainfall plays a crucial role are weather forecasting, agricultural planning, vector-borne and waterborne diseases (e.g., Rinaldo et al., 2012; Thaler et al., 2018).

Three different techniques can be used for estimating rainfall: ground measurements, meteorological modelling and remote sensing. Ground measurements are based on rain gauges and meteorological radars (Lanza et al., 2009), but also new approaches such as microwave links are being developed (e.g., Overeem et al., 2011). These measurements guarantee high accuracy but suffer in many regions from limited spatial coverage (Kidd et al., 2017). Alternatively, meteorological models are used to estimate rainfall mainly in areas without ground reliable observations (Ebert et al., 2007), e.g., reanalysis. The uncertainties associated with these estimates can be large, mainly in areas where ground observations are scarce (Massari et al., 2017a). Therefore, to fill the gaps in the spatial coverage of ground measurements, and to improve the estimates obtained by models, different remote sensing techniques have been developed in the last 30 years (Hou et al., 2014). The standard methods for estimating rainfall from space are based on instantaneous measurements obtained from microwave radiometers, radars, and infrared sensors (Kidd and Levizzani, 2011). These methods are based on inversion techniques where the upwelling radiation (or backscattered signal for radars) is related to the surface precipitation rate, i.e., a “top down” approach (Brocca et al., 2014).

The most recent and successful example of satellite precipitation estimates is represented by the Integrated Multi-Satellite Retrievals for Global Precipitation Measurement, GPM (IMERG) of the GPM mission (Hou et al., 2014) which provide high spatial (0.1°) and temporal
(30-minute) resolution and quasi-global coverage (+/-60°). To obtain such resolution and coverage, the IMERG products use a constellation of polar and geostationary satellite sensors operating in the microwave and infrared bands. However, the use of multiple sensors has some problems, including: the inconsistency between rainfall estimates from different sensors (intercalibration problem), the difficulties in collecting observations from multiple space agencies (i.e., problem of delivering the products in near real-time), and the high costs for the operation and the maintenance of the overall constellation. Moreover, as the top down approach requires the merging of instantaneous rainfall measurements from multiple sensors, the failure of one of them may imply a significant degradation in the accuracy of accumulated rainfall estimate due to the high temporal variability of rainfall (Trenberth and Asrar, 2014).

In recent years, a new “bottom up” approach has emerged that uses satellite soil moisture observations to infer, or to correct, rainfall over land (Brocca et al., 2013a; Crow et al., 2009; Pellarin et al., 2013; Wanders et al., 2015). The major difference between the bottom up and top down approaches is in the type of measurement; i.e., accumulated rainfall with the bottom up method and instantaneous rainfall rates with the top down method. This difference makes the two approaches highly complementary and their integration has been already successfully tested and demonstrated in several recent studies (e.g., Brocca et al., 2016; Ciabatta et al., 2017; Chiaravallotti et al., 2018; Massari et al. 2019). When accumulated rainfall estimates are needed (e.g., daily rainfall), the bottom up approach has the advantage of requiring a much lower number of measurements and, hence, of satellite sensors. The limitations of the bottom up approach are the possibility to estimate only terrestrial rainfall and its dependence on land characteristics (e.g., low accuracy for dense vegetation coverage and complex topography, Brocca et al., 2014).

The bottom up approach has been applied over a range of scales: global (Crow et al., 2011; Brocca et al., 2014; Ciabatta et al., 2018), continental (Wanders et al., 2015; Brocca et al., 2016), and local (Massari et al., 2014; Brocca et al., 2015; Román-Cascón et al., 2017) scale. Moreover, different satellite soil moisture products have been considered including SMOS (Soil Moisture Ocean Salinity mission, Brocca et al., 2016), ASCAT (Advanced SCATterometer, Brocca et al., 2017), AMSR-E (Advanced Microwave Scanning Radiometer, Crow et al., 2009), and SMAP (Soil Moisture Active and Passive, Koster et al., 2016; Tarpanelli et al., 2017; Zhang et al., 2019). First studies employing satellite rainfall estimates obtained through the bottom up approach for hydrological and water resources applications have been recently published (e.g.,
These studies have highlighted the large potential of this technique as a complimentary and useful approach for estimating rainfall from space, and have also shown its main limitations. Specifically, the temporal resolution and the accuracy of satellite soil moisture products play a fundamental role in determining the accuracy of the bottom up rainfall estimates.

In this study, we describe the newly developed SM2RAIN-ASCAT rainfall data record covering the period 2007-2018 and characterized by a spatial/temporal sampling of 12.5 km/1-day. The new SM2RAIN-ASCAT data record is obtained from the application of SM2RAIN algorithm (Brocca et al., 2014) to the ASCAT soil moisture data records H113 and H114 provided by the European Organisation for the Exploitation of Meteorological Satellites (EUMETSAT) Satellite Application Facility on Support to Operational Hydrology and Water Management (HSAF). It is the first SM2RAIN-ASCAT data record available at the same spatial resolution as the ASCAT soil moisture product (previous data records have been undersampled at 0.5- and 1-degree resolution). Moreover, we have included the latest improvements in pre- and post-processing of soil moisture and rainfall data as well as in the SM2RAIN algorithm. The main differences with the SM2RAIN-CCI rainfall data record (Ciabatta et al., 2018) are the input soil moisture product (the input of SM2RAIN-CCI is the European Space Agency Climate Change Initiative Soil Moisture, ESA CCI soil moisture, product, Dorigo et al., 2017), and the time coverage (SM2RAIN-CCI spans the period 1998-2015). Technically, the use of the same satellite sensor in SM2RAIN-ASCAT data record is preferable to ensure consistency between soil moisture estimates over time to which the SM2RAIN algorithm is highly sensitive.

The purpose of this study is twofold. As a first objective, we have applied SM2RAIN algorithm at 1009 points uniformly distributed (with spacing of 1.5°) in the United States, Italy, India and Australia for testing different configurations of data pre-/post-processing and SM2RAIN model equation. This analysis has allowed us to select the best configuration that is implemented on a global scale for obtaining the SM2RAIN-ASCAT data record. The second objective is the assessment of the global scale SM2RAIN-ASCAT data record through the comparison with reference datasets and by exploiting the Triple Collocation (TC) approach (Massari et al., 2017a). As reference datasets we have used high-quality local raingauge networks from 2013 to 2017 in the United States, Italy, India and Australia for the assessment at 1009 points and for the regional assessment. Three additional global datasets have been
considered: the latest reanalysis of the European Centre for Medium-Range Weather Forecasts (ECMWF), ERA5, the gauge-based Global Precipitation Climatology Centre (GPCC), and the GPM IMERG product (Early Run version). ERA5 has been used for the generation of the quasi-global SM2RAIN-ASCAT data record; GPCC and GPM IMERG have been considered for the TC analysis.

We underline that the paper goal is to present and describe the SM2RAIN-ASCAT quasi-global rainfall data record and to perform a comparison with state-of-the-art global rainfall products. We do not want to show a comprehensive assessment of the product. Indeed, we believe that researchers other than the product developers should perform the validation of the dataset. Even better, we stress the importance of performing the validation by using the datasets in hydrological or agricultural applications (e.g., flood prediction and agricultural water management).

2 Datasets

Nine different datasets have been collected for this study which are based on remote sensing, ground observations and reanalysis. Refer to Table 1 for a summary of the datasets.

The main input dataset for producing SM2RAIN-ASCAT data record is the ASCAT soil moisture data record provided by the “EUMETSAT Satellite Application Facility on Support to Operational Hydrology and Water Management (H SAF)” (http://hsaf.meteoam.it/). ASCAT, currently on board Metop-A (launched on October 2006), Metop-B (September 2012) and Metop-C (November 2018) satellites, is a scatterometer operating at C-band (5.255 GHz) and, by using the TU Wien algorithm (Wagner et al., 2013) the H SAF provides a soil moisture product characterized by 12.5 km spatial sampling. The temporal sampling is varying as a function of latitude and the number of satellites: by using Metop-A only a daily sampling is obtained, by using Metop-A and Metop-B two observations per day are available at mid-latitudes. Here we have used the H SAF ASCAT soil moisture data record (using Metop-A and Metop-B) available through the product H113 (PUM, 2018) covering the period 2007-2017 and its extension product H114 for the year 2018.

Three datasets obtained from the latest reanalysis of ECMWF, i.e., ERA5, have been used. ERA5 reanalysis is characterized by a spatial resolution of ~36 km and hourly temporal resolution. ERA5 is available from the Copernicus Climate Change service and the datasets cover the period 1979 to present. We have extracted hourly observations for the period 2007-
2018 for three variables: evaporation, soil temperature for the first layer (0-7 cm) and total rainfall (computed as the difference between total precipitation and snowfall). Evaporation data are used as additional input to the SM2RAIN algorithm and soil temperature data for masking periods with frozen soils. Total rainfall has been considered as a benchmark for the calibration of global SM2RAIN parameter values (see next section).

Ground-based rainfall datasets from regional networks have been also collected including the Climate Prediction Center (CPC) Unified Gauge-Based Analysis of Daily Precipitation in the United States, the gridded rainfall data provided by ~3000 stations of the National Department of Civil Protection in Italy (Ciabatta et al., 2017), the India Meteorological Department (IMD, http://www.imd.gov.in/pages/services_hydromet.php) rainfall observations in India, and the Australia Water Availability Project (AWAP, http://www.bom.gov.au/jsp/awap/rain/index.jsp) gridded rainfall data in Australia. These datasets have been used firstly for the selection of the optimal configuration of SM2RAIN implementation. For that, 1009 points uniformly distributed over the four regions have been selected. Secondly, the regional networks have been used for the assessment of the global SM2RAIN-ASCAT rainfall product at regional scale.

The ERA5 and local rainfall datasets have been regridded over the ASCAT grid (12.5 km) through the nearest neighbouring method and resampled at daily time scale as accumulated rainfall from 00:00 to 23:59 UTC. The ERA5 evaporation and soil temperature data are also regridded to the same grid and aggregated at daily scale as accumulated and average value from 00:00 to 23:59 UTC, respectively.

For the global assessment of SM2RAIN-ASCAT, two additional rainfall datasets have been considered: Global Precipitation Climatology Centre (GPCC) Full Data Daily Product (Schamm et al., 2015) and GPM IMERG Early Run product (Hou et al., 2014), hereinafter referred to as GPM-ER. Due to the availability of GPM-ER from April 2014, the global analysis has been carried out in the 4-year period from January 2014 to December 2018. Moreover, for the global inter-comparison all the datasets (SM2RAIN-ASCAT, ERA5, GPCC, and IMERG-ER) have been regridded at 0.25-degree resolution by spatially averaging the pixels contained in each 0.25-degree cell for SM2RAIN-ASCAT and GPM-ER, and by selecting the nearest pixel for ERA5 and GPCC.
3 Methods

In the following, the methodology used for obtaining the SM2RAIN-ASCAT data record is described. Specifically, three steps are carried out (see Figure 1): 1) surface soil moisture data pre-processing, 2) SM2RAIN algorithm, and 3) rainfall data post-processing. Different configurations for the data pre-/post-processing and for the SM2RAIN model equation are considered; the details are given in Table 2.

3.1 Soil moisture data pre-processing

The ASCAT surface soil moisture product is provided as relative soil moisture (between 0 and 1) at the overpass time of the satellite sensor (see Figure A1 for the mean daily revisit time of ASCAT in the period 2007-2012 with only Metop-A and the period 2013-2018 with Metop-A+B). For the application of SM2RAIN algorithm, data should be equally spaced in time and hence, we have linearly interpolated in time soil moisture observations every 24 hours, 12 hours and 8 hours. The interpolation may increase the risk of false rainfall events, but it is a required step to obtain accumulated rainfall over a fixed duration. In a preliminary test (not shown for brevity), we have tested the three sampling frequencies with the baseline formulation for SM2RAIN (equation 6, see below). The best performances have been obtained with 12 hours sampling, particularly from 2013 to 2018 in which both Metop-A and -B are available. Therefore, 12 hours sampling has been used in the following analyses. The 24-hour accumulated rainfall is obtained by summing the two 12-hour accumulated rainfall data obtained for each day.

One of the major problems in using satellite soil moisture observations for rainfall estimation is related to the high frequency fluctuations caused by measurement and retrieval errors. If positive, such fluctuations are interpreted erroneously as rainfall by SM2RAIN algorithm. Therefore, satellite surface soil moisture data need to be filtered before being used as input into SM2RAIN. In previous studies, the exponential filtering has been considered (Wagner et al., 1999). The exponential filter, also known as Soil Water Index (SWI), has been used for filtering surface soil moisture time series as a function of a single parameter, $T$, i.e., the characteristic time length. In this study, we have tested two additional filtering methods. The first one is an extension of the exponential filter in which the $T$ parameter is assumed to be varying with soil moisture as proposed in Brocca et al. (2013b). Specifically, $T$ decreases with increasing soil moisture through a 2-parameter power law. Therefore, the data are filtered more
during dry conditions. The third approach that we have implemented is a discrete wavelet filter (similar to Massari et al., 2017b). The discrete wavelet filter cuts the higher frequencies of the signal, typically characterized by noises, over a threshold selected through the principle of Stein's Unbiased Risk at multiple levels. We have found the Daubechies wavelets to be the most appropriate functions because their shape and the shape of the soil moisture signal is similar. Therefore, we have implemented a Daubechies-based wavelet filter in which the filtering level is optimized.

For all the filtering approaches, the parameter values of the filters have been optimized point-by-point in order to reproduce the reference rainfall observations.

### 3.2 SM2RAIN algorithm and calibration

The SM2RAIN algorithm is based on the inversion of the soil water balance equation and allows to estimate the amount of water entering the soil by using as input soil moisture observations from in situ or satellite sensors (e.g., Brocca et al., 2013a; 2014; 2015; Koster et al., 2016; Ciabatta et al., 2017; Massari et al., 2014). Specifically, the soil water balance equation can be described by the following equation (over non-irrigated areas):

\[ nZ \frac{ds(t)}{dt} = p(t) - g(t) - sr(t) - e(t) \]  

(1)

where \( n \) [-] is the soil porosity, \( Z \) [mm] is the soil layer depth, \( S(t) \) [-] is the relative saturation of the soil or relative soil moisture, \( t \) [days] is the time, \( p(t) \) [mm/day] is the rainfall rate, \( g(t) \) [mm/day] is the drainage (deep percolation plus subsurface runoff) rate, \( sr(t) \) [mm/day] is the surface runoff rate and \( e(t) \) [mm/day] is the actual evapotranspiration rate.

For estimating the rainfall rate, **equation (1)** is applied only during rainfall periods and, hence, some of the components of the equation can be considered as negligible. For instance, the actual evapotranspiration rate during rainfall is quite low due to the presence of clouds and, hence, the absence of solar radiation. Similarly, the surface runoff rate, i.e., the water that does not infiltrate into the soil and flows at the surface to the watercourses, is much lower than the rainfall rate, mainly if **equation (1)** is applied at coarse spatial resolution (20 km), i.e., with satellite soil moisture data. Indeed, most of water becomes runoff flowing in the subsurface, and also the part that does not infiltrate, due to for instance impervious land cover or soil, may re-infiltrate downstream within a pixel at 20 km scale. We have indirectly tested this hypothesis by counting the number of days the ASCAT soil moisture product is higher than 99.5 percentile.
for two (or more) consecutive days in the period 2007-2018. We have indirectly tested this hypothesis by counting the number of days the ASCAT soil moisture product is higher than 99.5 percentile for two (or more) consecutive days in the period 2007-2018. We have found that the number of consecutive days in which the soil is saturated is equal to 4 days (median value on a global scale) over 12 years, with 90% of land pixels with values lower than 12 days (i.e., 1 day per year). The occurrence of higher values is limited to very few areas in the tropical forests and over Himalaya (see Figure A2).

Following the indications obtained in Brocca et al. (2015), we have assumed the surface runoff rate, \( sr(t) \), as negligible (i.e., Dunnian runoff) and we have rearranged equation (1) for estimating the rainfall rate:

\[
p(t) = nZ \frac{dS(t)}{dt} + g(t) + e(t) \tag{2}
\]

In this study, we have considered different formulations for equation (2) by varying the drainage rate as:

\[
g(t) = K_s S(t)^m \tag{3.1}
\]

\[
g(t) = K_s S(t)^{\lambda+1} \left[ 1 - \left(1 - S(t)^{\frac{\lambda+1}{\lambda}} \right)^{\frac{\lambda}{\lambda+1}} \right]^2 \tag{3.2}
\]

\[
g(t) = K_s S(t)^{\tau} \left[ 1 - \left(1 - S(t)^{\frac{1}{m}} \right)^{\frac{1}{m}} \right]^2 \tag{3.3}
\]

where \( K_s \) [mm/day] is the saturated hydraulic conductivity, \( m [-] \) and \( \lambda [-] \) are exponents related to the pore size distribution index, and \( \tau \) is the tortuosity index. Specifically, the three equations represent the hydraulic conductivity - soil moisture formulation by Brooks-Corey (3.1), van Genuchten (3.2), and Mualem-van Genuchten (3.3).

The actual evapotranspiration rate has been considered as an additional input, together with soil moisture, here obtained from ECMWF reanalysis ERA5:

\[
e(t) = K_c ET_{ERA5}(t) \tag{4}
\]

where \( ET_{ERA5}(t) \) [mm/day] is the actual evapotranspiration rate obtained from ERA5 reanalysis and \( K_c [-] \) is a correction factor for taking into account potential bias in ERA5 estimates.
Moreover, we have considered an additional formulation in which $Z$ is a function of soil moisture taking into account the different penetration depth of satellite sensors as a function of wetness conditions:

$$Z = Z[0.1 + (1 - S(t)^c)]$$  \hspace{1cm} (5)

where $c$ exponent determines the rate of decrease of penetration depth with increasing soil moisture.

Accordingly, we have used different formulations for equation (2) that are compared with the baseline equation used in previous studies (e.g., Brocca et al., 2014):

$$p(t) = Z n \frac{ds(t)}{dt} + K_s S(t)^m$$  \hspace{1cm} (6)

In synthesis, we have investigated 3 different configurations (total of 5 options) for: 1) selecting the best equation for the drainage rate (equations 3), 2) testing the possibility to include the evapotranspiration component (equation 4), and 3) testing the use of a variable penetration depth with soil moisture conditions (equation 5). Each new configuration has been compared with the baseline (equation 6) in order to select the best configuration for SM2RAIN algorithm (see Figure 1). For all configurations, negative rainfall values, that might occur during some dry-down cycles, have been set equal to zero.

SM2RAIN parameter values are calibrated point-by-point by using the reference rainfall as target. As objective function, we have used the minimization of the RMSE between SM2RAIN-ASCAT and reference rainfall.

### 3.3 Rainfall data post-processing

The use of satellite soil moisture observations for obtaining rainfall estimates is affected by errors in the input data and in the retrieval algorithm SM2RAIN. The correction of the overall bias in the climatology is a simple and effective approach for mitigating part of such errors. Specifically, we refer here to a static correction procedure that once calibrated for a time period can be applied in the future periods, also for operational real time productions. We note that a climatological correction is performed in several satellite rainfall datasets delivered in near real-time (e.g., GPM-Early Run). We have implemented two different approaches for climatological correction: 1) a cumulative density function (CDF) matching approach at daily time scale, and 2) a monthly correction approach. Specifically, the implemented CDF matching approach is a 5-order polynomial correction as described in Brocca et al. (2011) for matching
the CDF of estimated rainfall with respect to reference rainfall, in which the CDF are computed
over the whole calibration period at daily time scale. The monthly correction approach
computes the monthly ratios between the climatology of estimated and reference rainfall, i.e.,
12 correction factors per pixel. Then, the SM2RAIN-estimated rainfall is multiplied for the
monthly correction factors to obtain the climatologically corrected SM2RAIN-estimated
rainfall.

### 3.4 Triple collocation analysis

For the global assessment of satellite, reanalysis and gauge-based rainfall products we
have used the Triple Collocation (TC) technique. TC can theoretically provide error and
correlations of three products (a triplet) given that each of the three products is afflicted by
mutually independent errors. Therefore, in principle, TC can be used for assessing the quality
of satellite products without using ground observations (Massari et al., 2017a). In this study,
we have implemented the same procedure as described in Massari et al. (2017), i.e., by
implementing an additive error model at daily time scale, and we refer the reader to this study
for the analytical details. In synthesis, by using the extended TC method firstly proposed by
McColl et al. (2014), it is possible to estimate the temporal correlation, \( R_{TC} \), of each rainfall
product in the triplets with the truth.

### 3.5 Performance scores

Several metrics have been used to assess the product performance during the validation
period. As continuous scores we have computed the Pearson’s correlation coefficient (\( R \)), the
root mean square error (RMSE), the mean error between estimated and reference rainfall
(BIAS), and the ratio of temporal variability of estimated and reference rainfall (STDRATIO).
Continuous scores have been computed on a pixel-by-pixel basis by considering 1 day of
accumulated rainfall. Moreover, three categorical scores, i.e. Probability of Detection (POD),
False Alarm Ration (FAR) and Threat Score (TS), have been computed. POD is the fraction of
correctly identified rainfall events (optimal value POD=1), FAR is the fraction of predicted
events that are non-events (optimal value FAR=0), while TS provides a combination of the
other two scores (optimal value TS=1). The categorical assessment is carried out by considering
a rainfall threshold of 0.5 mm/day (instead of 0 mm/day) in order to exclude spurious events
that might be due to rainfall interpolation/regridding in the reference datasets. For a complete
description of the performance scores, see Table A1 in the Appendix.
4 Results

The results are split in three parts: 1) selection of the optimal configuration of SM2RAIN through the assessment at 1009 points, 2) generation of global SM2RAIN-ASCAT rainfall data record, and 3) regional assessment of SM2RAIN-ASCAT with gauge-based rainfall datasets and global assessment through TC.

4.1 Selection of the best SM2RAIN processing configuration at 1009 points

As a first step we have co-located satellite soil moisture data from ASCAT soil moisture H113+H114, ground-based rainfall observations and actual evapotranspiration data from ERA5 in space and time at 1009 points. We have selected 1009 points uniformly distributed over a regular grid with spacing of 1.5°. Each point is considered representative of a 0.25° x 0.25° box. The selection is carried out for reducing the computational time in running the different SM2RAIN configurations. The numbers of points for each region is depending on the size of the region: 328 points in Australia, 163 in India, 55 in Italy, and 463 in the United States. Ground observations, GPM-ER and ERA5 data are regridded by spatial averaging measurements contained over each 0.25° x 0.25° box. These datasets are made freely available here (https://doi.org/10.5281/zenodo.2580285, Brocca, 2019) for those interested to test alternative approaches for rainfall estimation from ASCAT soil moisture. Specifically, we have considered the period 2013-2016, 2013-2014 for the calibration and 2015-2016 for the validation; in the sequel only the results in the validation period are shown. The ground-based high quality rainfall observations available for the four regions are used as reference data (ground truth) in this analysis. The reference configuration, REF, as used in previous SM2RAIN applications (e.g., Brocca et al., 2014), uses the SWI for data filtering, the SM2RAIN formulation as in equation (6), and no climatological correction. Results in the validation period are shown in Figure 2A in terms of temporal R against reference data. As shown, the median R for all points is equal to 0.60, with better results in Italy (median R=0.67, see boxplots) and similar results in the other 3 regions (median R=0.60 and 0.59). These results are in line with previous studies (e.g., Ciabatta et al., 2017; Tarpanelli et al., 2017) carried out in Italy and India and highlight the potential of ASCAT soil moisture observations to provide daily rainfall estimates. Figure 3 (first column) shows the results for the different performance metrics; in the last two columns the results obtained with GPM-ER and ERA5 are shown for comparison. Very good statistics have been obtained in terms of RMSE and BIAS but a tendency to underestimate the observed rainfall variability (median STDRATIO=0.60) and medium-high
probability of false alarm (median FAR=0.53). The other scores are similar, or slightly lower than those obtained through GPM-ER and ERA5.

The first test has been dedicated to the filtering of soil moisture data by using three approaches: 1) SWI, i.e., the REF configuration, 2) SWI with T varying with soil moisture, SWI-Tvar, and 3) the discrete wavelet filtering, WAV. **Figure 3** shows in the first three columns the summary of the performance scores highlighting that the SWI-Tvar configuration is performing the best, even though the differences with REF configuration are small. **Figure 2b** shows the R map for SWI-Tvar configuration while in **Figure 2c** the differences in R-values with REF are displayed. Improved performance in terms of R is visible over most of the pixels except in central Australia.

The second test has been performed on the SM2RAIN equation by using different drainage functions (VGEN and MUA configurations), by adding the evapotranspiration component (EVAP), and by considering the variability of sensing depth, Z, with soil moisture (ZVAR). VGEN, MUA and ZVAR configurations are characterized by lower performances than REF (see **Figure 3**, columns 4, 5 and 7), even though MUA and ZVAR incorporate an additional parameter to be calibrated (and, hence, better performance was expected). The addition of evapotranspiration brings a slight improvement with respect to REF (see **Figure 3**, column 6), with results similar to SWI-Tvar. Larger improvements are obtained over areas in which evapotranspiration is more important, e.g., in the south-western United States and central western Australia. In India and Italy, the results are very similar to REF. However, EVAP configuration requires actual evapotranspiration data from ERA5 as additional input and such data might be not available for the implementation of the processing algorithm in an operational context.

The final test has been done by applying the daily CDF matching, BC-CDF, and monthly correction factors, BC-MON, for correcting the climatological bias in SM2RAIN-derived rainfall estimates; results are shown in columns 8 and 9 of **Figure 3**. For these two configurations, the improvements with respect to REF are evident but with different magnitude for the different scores. BC-CDF improves significantly STDRATIO, TS and FAR with a slight deterioration in R and RMSE. BC-MON shows the highest R-values among all configurations with the larger improvements in India, Italy and United States. However, the improvement in terms of STDRATIO, TS and FAR is less important than BC-CDF. Therefore, depending on which score is assumed more important, one of the two configurations can be selected. If
compared with GPM-ER, BC-CDF and BC-MON configurations show similar results with larger positive differences, in terms of RMSE, BIAS, STDRATIO and POD; R values are slightly better for GPM-ER that is also much better in terms of TS and FAR. Similar findings can be summarized in the comparison with ERA5, even though ERA5 is performing the best in terms of R, STDRATIO, FAR, and TS among all configurations.

*Figure 4* shows time series of rainfall averaged over the four regions as obtained from ground observations and from BC-MON configuration. The agreement of spatially averaged rainfall with observations is high with R-values greater than 0.83, and very low BIAS. Moreover, regional scale rainfall events are correctly reproduced both in terms of timing and magnitude.

### 4.2 Generation of SM2RAIN-ASCAT data record

Based on the tests performed in the previous paragraph, we have selected the best configuration using SWI-Tvar for filtering, Brooks-Corey function for losses, and the monthly correction approach for climatological correction. The addition of evapotranspiration component, even though showing some improvements, has been not used in view of an operational implementation of the method. The monthly correction approach has been selected as R and RMSE scores have been considered more important based on previous investigations on the assessment of satellite rainfall products (e.g., Massari et al., 2017).

The selected configuration has been applied on a global scale to 839826 points over which ASCAT soil moisture observations are available. As reference dataset for the calibration of the parameter values of the pre-processing (filtering), of SM2RAIN, and of the post-processing, the ERA5 rainfall has been used mainly because of its higher spatial resolution compared to GPCC (36 km versus 100 km). However, we have also tested the use of the two datasets for calibration at randomly chosen 20000 points which showed that the estimated rainfall in the two calibration tests is very similar. For instance, the median R between the two SM2RAIN-ASCAT data records is higher than 0.90 (not shown for brevity). This result clearly demonstrate that the selection of reference dataset has a small influence on SM2RAIN-derived rainfall that is mostly driven from soil moisture temporal fluctuations. Additionally, considering the improved ASCAT coverage after 2013, the calibration has been split from 2007 to 2012 (Metop-A) and from 2013 to 2018 (Metop-A and -B). The dual calibration has solved the issue in terms of long-term trend that has been found in previous application of SM2RAIN to ASCAT
soil moisture data (Beck et al., 2017). Finally, we have flagged rainfall observations in space and time when the data are supposed to be less reliable. In space (i.e., a fixed spatial mask), we have used the committed area mask developed for the ASCAT soil moisture product (i.e., the area in which the ASCAT soil moisture retrievals are expected to be good, PVR 2017), a frozen probability mask and a topographic complexity mask. In time (i.e., a temporally variable mask), we have considered the soil temperature data from ERA5 and flagged the observations with soil temperature values between 0°C and 3°C as temporary frozen soil and below 3°C as frozen soil. As many applications require continuous data, we have preferred to flag the data instead of removing them with an expected loss of accuracy.

The SM2RAIN-ASCAT data record so obtained has a spatial sampling of 12.5 km, a daily temporal resolution and covers the 12-year period 2007-2018. Figure 5 shows R and RMSE values between SM2RAIN-ASCAT and ERA5 in a single map. Therefore, Figure 5 illustrates the consistency between SM2RAIN-ASCAT and ERA5, and it is not intended to assess the performance of the data record (even though we expect better accuracy in areas where the agreement is higher). Green light colours indicate very good agreement with high R and low RMSE, orange to red colours indicate low R and high RMSE, while black colour indicates low RMSE and R highlighting areas in which rainfall occurrence and variability is very low (e.g., Sahara Desert, high latitudes). The data record has been found in very good agreement with ERA5 (high R and low RMSE) in western United States, Brazil, southern and western South America, southern Africa, Sahel, southern-central Eurasia, and Australia. The areas in which SM2RAIN-ASCAT is characterized by lower consistency with ERA5 are those with dense vegetation (Amazon, Congo, and Indonesia), with complex topography (e.g., Alps, Himalaya, Andes), at high latitudes and Saharan and Arabian deserts. In these areas it is well-known that the ASCAT soil moisture product has limitations (e.g., Wagner et al., 2013), and generally the retrieval of soil moisture from remote sensing is more challenging. The median R and RMSE values are equal to 0.56 and 3.06 mm/day, with slightly better scores in the period 2013-2018 (R=0.57, RMSE=2.95), thanks to the availability of ASCAT on both Metop-A and Metop-B.

4.3 Regional and global assessment of SM2RAIN-ASCAT data record

By using all the pixels included in the four regions (Italy, United States, India and Australia), for a total of 29843 points, the new SM2RAIN-ASCAT rainfall data record has been compared with reference rainfall observations in Figure 6, by considering the whole period 2007-2018. Specifically, the box plots of different performance metrics (the same of Figure 3)
are shown and compared with the results obtained through GPCC, ERA5, and GPM-ER. By focusing on the SM2RAIN-ASCAT data record performance over the different regions, it shows better performance in Italy (median $R=0.67$) and United States (median $R=0.62$), almost comparable with the other datasets; while in Australia and India $R$-values are lower (median $R=0.61$ and 0.59). In the selected regions, the best product is GPCC (mainly in Australia) followed by ERA5 while GPM-ER and SM2RAIN-ASCAT are performing similarly in terms of $R$. The better performance of GPCC are expected (gauge-based dataset) and also the very good performance of ERA5 in Italy and Australia thanks to the availability of ground observations for the reanalysis. We highlight also that differently from SM2RAIN-ASCAT and GPM-ER, GPCC and ERA5 have a latency of weeks to months and, hence, these products cannot be used for near real time applications. When considering the RMSE score, the results are quite different with respect to $R$. SM2RAIN-ASCAT is overall very good being the best (second best) product in United States (India). The ranking of the product is GPCC, SM2RAIN-ASCAT, ERA5 and GPM-ER, with the latter showing high RMSE values in United States and Australia. As obtained in previous studies (Brocca et al., 2016; Ciabatta et al., 2017), the SM2RAIN approach is very good in obtaining low RMSE values thanks to its accuracy in the retrieval of accumulated rainfall. Moreover, the product accuracy is stable over time as it is not as strongly affected by the availability of satellite overpasses as in the top down approach. As shown also in Figure 3, the SM2RAIN-ASCAT data record has limitations in reproducing the variability of rainfall (low STDRATIO) mainly due underestimation issues. Moreover, FAR values of SM2RAIN-ASCAT are quite high highlighting the difficulties in removing the problem of high frequency soil moisture fluctuations wrongly interpreted by SM2RAIN as rainfall events.

On a global scale, the TC approach has been implemented by using the triplet SM2RAIN-ASCAT, GPM-ER and GPCC, by considering the common period 2015-2018 and at daily time scale. In TC analysis we have not considered ERA5 purposely to avoid any dependency between the products. Theoretically, the extended TC approach provides the correlation, $R_{TC}$, against the underlying “truth”. Figures 7A and 7B show the $R_{TC}$ maps for SM2RAIN-ASCAT and GPM-ER highlighting similar mean values (0.66 and 0.64 for SM2RAIN-ASCAT and GPM-ER, respectively). It should be underlined that the $R_{TC}$ values are higher than those obtained in the comparison with ground observations as theoretically the metric does not contain the error in the reference (Massari et al., 2017a). The spatial pattern of the performance is quite different as demonstrated in Figure 7c in which the differences between the two $R_{TC}$
maps is shown. Again, these results underline the strong complementarity between bottom up and top down approaches (e.g., Ciabatta et al., 2017; Chiaravallotti et al., 2018). As expected, SM2RAIN-ASCAT performs worse over desert areas, tropical forests and complex mountainous regions. Differently, over plains and low vegetated areas SM2RAIN-ASCAT is performing better than GPM-ER, particularly in the southern hemisphere. Indeed, in Africa and South America SM2RAIN-ASCAT provides good performance (see also Figure 7A) thanks to the capability of the bottom up approach to estimate accumulated rainfall accurately with a limited number of satellite overpasses occurring in these areas, differently from the top down approach used in GPM-ER.

The box plots of R\textsubscript{TC} shown in Figure 7D indicates that, overall, GPCC is performing similar to the two satellite products with major differences in the spatial patterns of the performance. SM2RAIN-ASCAT is performing the best among the three products in Africa, South America, central-western United States and central Asia while GPCC is performing the best in the remaining parts except the tropical region in which GPM-ER is performing very good (see Figure 8). If we consider only the committed area of ASCAT (PVR 2017), in which the soil moisture product is supposed to be reliable, the mean value of R\textsubscript{TC} is equal to 0.72 whereas in the masked area it is equal to 0.59.

5 Data availability

The SM2RAIN-ASCAT data record is freely available at https://doi.org/10.5281/zenodo.2591215 (Brocca et al., 2019).

6 Conclusions

In this study, we have described the development of a new SM2RAIN-ASCAT rainfall data record highlighting the steps carried out for improving the retrieval algorithm and the pre-/post-processing of the data. The major novelties of the SM2RAIN-ASCAT rainfall data record developed here with respect to previous versions are: 1) application of SM2RAIN at full spatial resolution thus providing a gridded data record with sampling of 12.5 km, 2) improved sampling and filtering of ASCAT soil moisture data, 3) application of monthly climatological correction, and 4) improved calibration strategy.

The SM2RAIN-ASCAT data record has been preliminary assessed at regional (Figures 4 and 6) and global (Figure 5, 7 and 8) scale in terms of different performance metrics with
larger emphasis on the temporal correlation, $R$, and the root mean square error, RMSE. The overall performances are good, mainly in terms of RMSE thanks to the capacity of SM2RAIN to accurately reproduce accumulated rainfall consistently over time. Importantly, SM2RAIN-ASCAT is found to perform even better than ground-based GPCC product over the southern hemisphere in Africa and South America, and in central-western United States and central Asia. Limitations of SM2RAIN-ASCAT data record consist in: 1) the underestimation of peak rainfall events, 2) the presence of spurious rainfall events due to high frequency soil moisture fluctuations, 3) the estimation of liquid rainfall only (snowfall cannot be estimated), and 4) the possibility to estimate rainfall over land only.

In the near future, we are going to develop the near real-time version of the SM2RAIN-ASCAT rainfall product that can be used as input for applications such as flood prediction (similarly to Camici et al., 2018 and Massari et al., 2018), landslide prediction (Brunetti et al., 2018) and novel applications for the agriculture and for the water resources management.

Acknowledgments: The authors gratefully acknowledge support from the EUMETSAT through the Global SM2RAIN project (contract n° EUM/CO/17/4600001981/BBo) and the “Satellite Application Facility on Support to Operational Hydrology and Water Management (H SAF)” CDOP 3 (EUM/C/85/16/DOC/15).


Table 1. List of satellite, ground-based and reanalysis products used in this study (the spatial/temporal sampling used in this study is reported).

<table>
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<tr>
<th>Short name</th>
<th>Full name and details</th>
<th>Data source</th>
<th>Spatial/temporal sampling</th>
<th>Time period</th>
<th>References</th>
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<td>reanalysis</td>
<td>0.25°/daily</td>
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Table 2. Configurations used in the paper (SWI: Soil Water Index, BCO: Brooks-Corey. VGE: van Genuchten, MUA: Mualem-van Genuchten, SWI-Tvar: SWI with T varying with soil moisture, WAV: wavelet filtering, CDF: climatological correction with daily cumulative density function matching, MON: climatological correction with monthly correction factors).

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Figure 1. Processing steps for obtaining the SM2RAIN-ASCAT global rainfall data record (2007-2018) from ASCAT surface soil moisture data: pre-processing, SM2RAIN algorithm, and post-processing. Each bullet represents a possible configuration that has been tested, the selected configuration is in red, bold font.
**Figure 2.** Performance of two different configurations at 1009 points in terms of Pearson’s correlation, R [-]. A) R map with reference configuration, B) R map with Soil Water Index (SWI) filtering with variable T as a function of soil moisture, and C) R map difference (B)-(A). The inner box plots show the R values (and R differences) split for different regions.
Figure 3. Performances at 1009 points in terms of Pearson’s correlation, $R [-]$, root mean square error, RMSE [mm/day], variability ratio, STDRATIO [-], BIAS [mm/day], false alarm ratio, FAR [-], Probability of Detection, POD [-], and Threat Score, TS [-]. For details of the different configurations see Table 2 (GPM-ER: GPM IMERG Early Run product).
Figure 4. Time series of mean areal rainfall for the four regions for observed data, OBS, and SM2RAIN-ASCAT data record, BC-MON configuration (R [-]: Pearson’s correlation, BIAS [mm/day]: mean error).
Figure 5. Pearson’s correlation, R, and root mean square error, RMSE, map of SM2RAIN-ASCAT data record compared with ERA5 reanalysis dataset used as benchmark (period 2007-2018). The analysis is carried out at 1-day and 12.5 km temporal and spatial resolution. The map shows that SM2RAIN-ASCAT data record is performing well in the western United States, Brazil, southern and western South America, southern Africa, Sahel, southern-central Eurasia, and Australia (green colours).
**Figure 6.** Regional assessment of SM2RAIN-ASCAT rainfall data record and comparison with GPCC, ERA5 and GPM-ER rainfall products. As reference the high-quality ground-based datasets in Italy, United States, India and Australia are used. Results in terms of Pearson’s correlation, R [-], root mean square error, RMSE [mm/day], variability ratio, STDRATIO [-], BIAS [mm/day], false alarm ratio, FAR [-], Probability of Detection, POD [-], and Threat Score, TS [-].
Figure 7. Global triple collocation, TC, results. A) $R_{TC}$ map for SM2RAIN-ASCAT, B) $R_{TC}$ map for GPM-ER, (C) differences between (A) and (B), i.e., blue (red) colours for pixels in which SM2RAIN-ASCAT (GPM-ER) is performing better, and D) box plot of $R_{TC}$ for SM2RAIN-ASCAT, GPM-ER, and GPCC. SM2RAIN-ASCAT is performing significantly better than GPM-ER in South America and Africa (excluding desert and tropical forest areas), elsewhere the two satellite products perform similarly.
Figure 8. Best performing product based on the results of triple collocation shown in Figure 7. SM2RAIN-ASCAT is performing the best among the three products in Africa, South America, central-western United States and central Asia while GPCC is performing the best in the remaining parts of the northern hemisphere and in Australia. GPM-ER is the best product in the tropical and equatorial region.
### Appendix

**Table A1.** Equations used for the performance scores. For the continuous scores, $P_{ref}$ is the reference dataset (e.g., ground observations, ERA5) and $P_{est}$ is the estimated dataset (e.g., SM2RAIN-ASCAT, GPM-ER), $cov$ is the covariance operator, $\sigma$ is the standard deviation operator, $\Sigma$ is the summation operator, and $N$ is the sample size. For the categorical scores, $H$ is the number of successfully predicted events by a given rainfall product, $F$ the number of non-events erroneously predicted to occur, and $M$ the number of actual events that are missed.

<table>
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<tr>
<td>Bias</td>
<td>BIAS</td>
<td>$BIAS = \frac{\Sigma(P_{est} - P_{ref})}{N}$</td>
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<tr>
<td><strong>Categorical scores</strong></td>
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<td>False Alarm Ratio</td>
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<tr>
<td>Probability of Detection</td>
<td>POD</td>
<td>$POD = \frac{H}{H + M}$</td>
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<tr>
<td>Threat Score</td>
<td>TS</td>
<td>$TS = \frac{H}{H + F + M}$</td>
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</table>
**Figure A1.** Mean daily revisit time [days] of ASCAT soil moisture observations for the period 2007-2012 (only Metop-A, top panel) and for the period 2013-2018 (Metop-A+B, bottom panel).
Figure A2. Number of days in which ASCAT soil moisture observations are close to saturation (>99.5 percentile, top panel) for 2 (or more) consecutive days in the period 2007-2018. Please note that the upper value is set to 20 days as in most of land areas the occurrence is very low (90% of land pixel with values lower than 12 days over 12 years). In the bottom panel the soil moisture values at 99.5 percentile (in the period 2007-2018) are shown.